Connection between Suprisal value S, a p-value of p and Binomial distribution:

 $S = -\log_2(p)$ $p = \frac{1}{2^S}$ p = Binom(S, S, 0.5)

S as an integer number

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$$S = \log_2\left(p^{-1}\right) \qquad p = \left(\frac{1}{2}\right)^S$$

$$p = \binom{S}{S} 0.5^S (1 - 0.5)^{S-S}$$

$$S = \log_2\left(\frac{1}{p}\right) \qquad p = 2^{-S}$$

$$p = \left(\frac{1}{2}\right)^S$$

Probability for S heads in a toss of S fair coins (Prob = 0.5)

 $2^S = \frac{1}{p}$